

CS 3721: Programming Languages Lab

Lab #10: Tail Recursion and Loops

Suppose we have the following function definition *length* in ML.

```
fun length(nil, result) = result
  | length(x::y, result) = length(y, result+1);
```

You can test the above function with the following invocation

```
- length ([2,3,4,5,7],0);
val it = 5 : int
```

The above *length* can be translated to the following loop implementation.

```
fun length(y) = let val result=ref 0; val p_y=ref y in
                  while not (!p_y = []) do
                    ( result := !result + 1; p_y := tl(!p_y) );
                  !result
                end;
```

Translate the following tail-recursive ML functions to loop implementations. Test your code by invoking both the original recursive implementation and your new implementation with a test input, and make sure they return the same result.

1.

```
fun Append(nil, ys) = ys
  | Append(x::xs, ys) = Append(xs, x::ys);
```
2.

```
fun Product([], res) = res
  | Product(x::y, res) = Product(y, x * res);
```
3.

```
fun gcd(x,y) = if x = y then x
               else if (x > y) then gcd(y, x-y) else gcd(x, y-x);
```