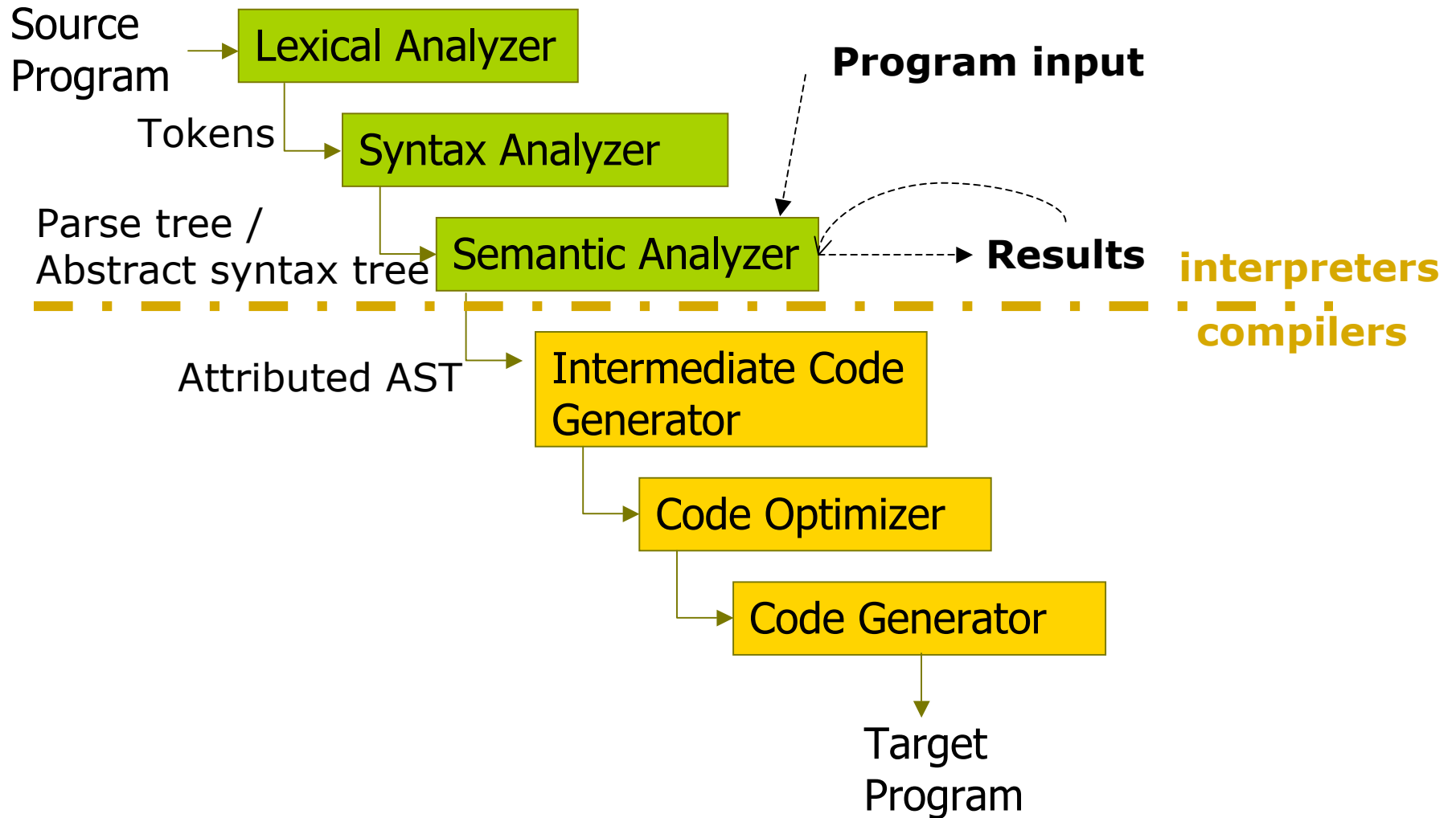


Intermediate Code Generation



Abstract syntax tree, three-
address code, and type
checking

Compile-time semantic evaluation



Intermediate code generation



- Static checker
 - Type checking, context-sensitive analysis
- Intermediate language between source and target
 - Multiple machines can be targeted
 - Attaching a different backend for each machine
 - Intel, PowerPC, UltraSparc can all share the same parser for C/C++
 - Multiple source languages can be supported
 - Attaching a different frontend (parser) for each language
 - Eg. C and C++ can share the same backend
 - Allow independent code optimizations
 - Multiple levels of intermediate representation
 - Low-level intermediate language: close to target machine
 - AST, post-fix, three-address code, stack-based code, ...

Type Checking

- Each operation in a language
 - Requires the operands to be predefined types of values
 - Returns an expected type of value as result
- When operations misinterpret the type of their operands, the program has a type error
 - function call `x()` where `x` is not a function
 - may cause jump to a illegal op code
 - `int_add(3, 4.5)`
 - It is an error to interpret bit pattern of 4.5 as an integer
- Compilers must determine a unique type for each expression
 - Ensure that types of operands match those expected by an operator
 - Determine the size of storage required for each variable
 - Calculate addresses of variable and array accesses

Type expressions

A type expression is

- a basic type (eg. bool, char, float, int, void)
- a type name
- or formed by applying type constructor to other expressions
 - Array type: $\text{array}(I,T) \rightarrow$ arrays with elements of type T and indices of type I.
 - `float a[100];` $\rightarrow a : \text{array}(\text{int}, \text{float})$
 - Tuple type: $T_1 * T_2 * \dots * T_n \rightarrow$ cartesian product of types T_1, T_2, \dots, T_n
 - `(int a, float b)` $\rightarrow (a,b) : \text{int} * \text{float}$
 - Record type: $\text{record}((fd_1 * T_1) * (fd_2 * T_2) \dots * (fd_n * T_n)) \rightarrow$ records with a sequence of fields fd_1, fd_2, \dots, fd_n of types T_1, \dots, T_n
 - `struct {int a,b;} xyz;` $\rightarrow xyz : \text{record}(a:\text{int} * b:\text{int})$
 - Pointer type: $\text{pointer}(T) :$ pointer to an object of type T
 - `double *p;` $\rightarrow p : \text{pointer}(\text{double})$
 - Function type $D \rightarrow T$: functions that map values of type D to values of type T
 - `int f (char* a, int b);` $\rightarrow f : \text{pointer}(\text{char}) * \text{int} \rightarrow \text{int}$

Structural equivalence of type expressions

- Two type expressions s and t are structurally equivalent if
 - s and t are the same basic type or
 - s and t are built using the same compound type constructor with the same components

```
Function structure-equiv(s, t) : boolean  
  if s and t are the same basic type  
    return true;  
  else if s == array(s1,s2) and t == array(t1,t2)  
    return structure-equiv(s1,t1) and structure-equiv(t1,t2)  
  else if s == record(s1) and t == record(t1)  
    return structure-equiv(s1, t1)  
  else if s == s1 * s2 and t == t1 * t2 then  
    return structure-equiv(s1,t1) and structure-equiv(t1,t2)  
  else if s == pointer(s1) and t == pointer(t1)  
    return structure-equiv(s1,t1)  
  else if s == s1 → s2 and t == t1 → t2  
    return structure-equiv(s1,t1) and structure-equiv(t1,t2)  
  else return false
```

Names for type expressions

- Type expressions can be given names and names can be used to define type expressions
 - `struct XYZ { int a, b,c; };`
 - `Struct abc { XYZ* p1, p2; };`
- Name equivalence
 - Each type name represent a different type
 - `struct XYZ {int a,b,c; }` and `struct ABC {int a,b,c;}` are different types

```
typedef Cell* Link;  
Link next, last;  
Cell* p, q, r;
```

**Do the variables all have identical types?
Yes if structural equivalence; no if name equivalence.**

Evaluating types of expressions

```
P ::= D ; E  
D ::= D ; D | id : T  
T ::= char | integer | T [ num ]  
E ::= literal | num | id | E mod E | E[E]
```

```
P ::= D ; E  
D ::= D ; D | id : T { addtype(id.entry, T.type); }  
T ::= char { T.type = char; } | integer { T.type = integer ;}  
      | T1[num] { T.type = array(num.val, T1.type);}  
E ::= literal { E.type = char; } | num { E.type = num; }  
      | id { E.type = lookupType(id.entry); }  
      | E1 mod E2 {if (E1.type == integer && E2.type==integer)  
                  E.type = integer; else E.type = type_error;}  
      | E1[E2] { if (E2.type == integer && E1.type==array(s,t))  
                  E.type = t; else E.type = type_error; }
```


Type checking with coercion

- Implicit type conversion
 - When type mismatch happens, compilers automatically convert inconsistent types into required types
 - $2 + 3.5$: convert 2 to 2.0 before adding 2.0 with 3.5

```
E ::= ICONST { E.type = integer; }  
E ::= FCONST { E.type = real; }  
E ::= id      { E.type = lookup(id.entry); }  
E ::= E1 op E2 { if (E1.type==integer and E2.type==integer)  
                  E.type = integer;  
                  else if (E1.type==integer and E2.type==real)  
                  E.type=real;  
                  else if (E1.type==real and E2.type==integer)  
                  E.type=real;  
                  else if (E1.type==real and E2.type==real)  
                  E.type=real;  
                  }  
}
```

Type checking of statements

```
P ::= D ; S  
D ::= D ; D | id : T  
T ::= char | integer | T [ num ]  
S ::= E ; | { S S } | if (E) S | while (E) S  
E ::= literal | num | id | E mod E | E[E]
```

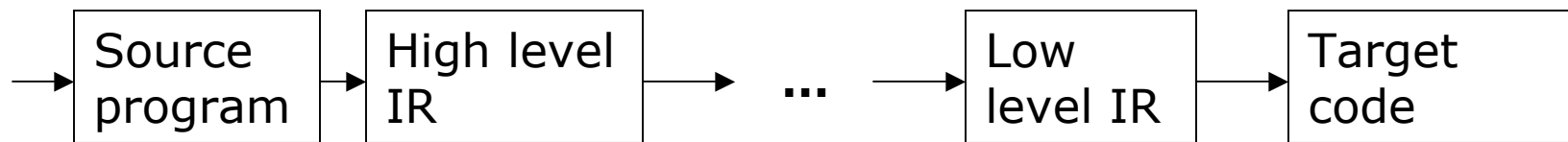
```
S ::= E ; { if (E.type!=type_error) S.type = void;  
          else S.type = type_error; }  
| '{' S1 S2 '}' { if (S1.type == void) S.type = S2.type;  
                  else S.type = type_error; }  
| if '(' E ') S1 { if (E.type == integer) S.type=S1.type;  
                  else S.type=type_error; }  
| while '(' E ') S1 { if (E.type == integer) S.type=S1.type;  
                  else S.type=type_error; }
```

Type checking of function calls

```
P ::= D ; E  
D ::= D ; D | id : T | T id (Tlist)  
Tlist ::= T, Tlist | T  
T ::= char | integer | T [ num ]  
E ::= literal | num | id | E mod E | E[E] | E(Elist)  
Elist ::= E, Elist | E
```

```
.....  
D ::= T1 id (Tlist) { addtype(id.entry, fun(T1.type, Tlist.type)); }  
Tlist ::= T, Tlist1 { Tlist.type = tuple(T1.type, Tlist1.type); }  
          | T { Tlist.type = T.type }  
E ::= E1 ( Elist ) { if (E1.type == fun(r, p) && p == Elist.type)  
                          E.type = r ; else E.type = type_error; }  
Elist ::= E, Elist1 { Elist.type = tuple(E1.type, Elist1.type); }  
          | E        { Elist.type = E.type; }
```

Intermediate representation



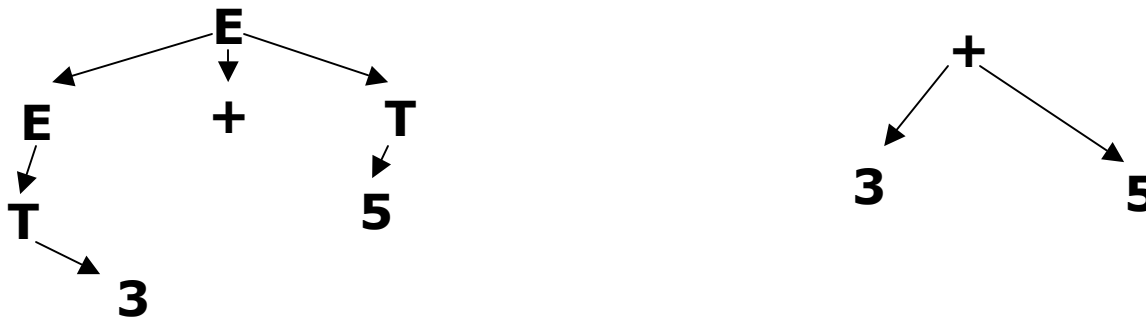
- A compiler might use a sequence of different IRs
 - High level IRs preserve high-level program structure
 - Eg., classes, loops, statements, expressions
 - Low level IRs support explicit expression and optimization of implementation details
- Selecting IR --- depends on the goal of each pass
 - Source-to-source translation: close to source language
 - Parse trees and abstract syntax trees
 - Translating to machine code: close to machine code
 - Linear three-address code
- External format of IR
 - Allows independent passes over IR

Abstract syntax tree

- Condensed form of parse tree for representing language constructs
 - Operators and keywords do not appear as leaves
 - They define the meaning of the interior (parent) node



- Chains of single productions may be collapsed



Constructing AST

Grammar:

$\begin{aligned} E &::= E + T \mid E - T \mid T \\ T &::= (E) \mid \text{id} \mid \text{num} \end{aligned}$

- Use syntax-directed definitions
 - Problem: construct an AST for each expression
 - Attribute grammar approach
 - Associate each non-terminal with an AST
 - Each AST: a pointer to a node in AST
E.nptr T.nptr
 - Definitions: how to compute attribute?
 - Bottom-up: synthesized attribute
if we know the AST of each child, how to compute the AST of the parent?

Constructing AST for expressions

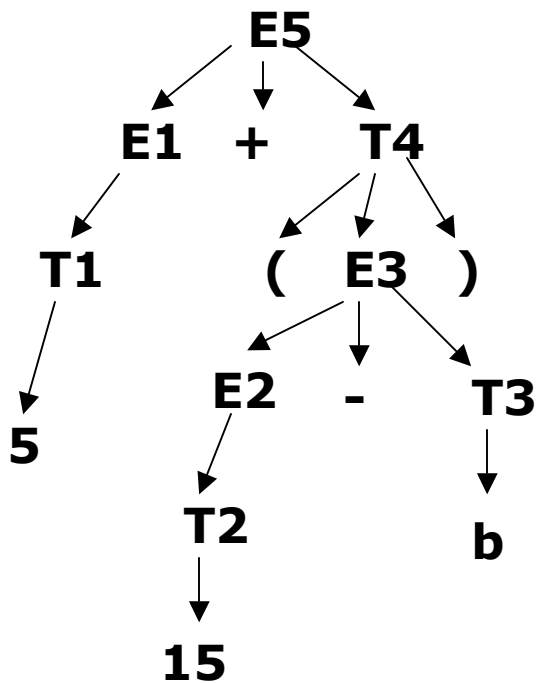
- Associate each non-terminal with an AST
 - E.nptr, T.nptr: a pointer to ASTtree
- Synthesized attribute definition:
 - If we know the AST of each child, how to compute the AST of the parent?

Production	Semantic rules
$E ::= E1 + T$	$E.nptr = \text{mknode_plus}(E1.nptr, T.nptr)$
$E ::= E1 - T$	$E.nptr = \text{mknode_minus}(E1.nptr, T.nptr)$
$E ::= T$	$E.nptr = T.nptr$
$T ::= (E)$	$T.nptr = E.nptr$
$T ::= \text{id}$	$T.nptr = \text{mkleaf_id}(\text{id.entry})$
$T ::= \text{num}$	$T.nptr = \text{mkleaf_num}(\text{num.val})$

Example: constructing AST

Bottom-up parsing: evaluate attribute at each reduction

Parse tree for $5+(15-b)$



1. reduce 5 to T1 using $T ::= \text{num}$:
T1.nptr = leaf(5)
2. reduce T1 to E1 using $E ::= T$:
E1.nptr = T1.nptr = leaf(5)
3. reduce 15 to T2 using $T ::= \text{num}$:
T2.nptr = leaf(15)
4. reduce T2 to E2 using $E ::= T$:
E2.nptr = T2.nptr = leaf(15)
5. reduce b to T3 using $T ::= \text{num}$:
T3.nptr = leaf(b)
6. reduce E2-T3 to E3 using $E ::= E-T$:
E3.nptr = node('-', leaf(15), leaf(b))
7. reduce (E3) to T4 using $T ::= (E)$:
T4.nptr = node('-', leaf(15), leaf(b))
8. reduce E1+T4 to E5 using $E ::= E+T$:
E5.nptr = node('+', leaf(5), node('-', leaf(15), leaf(b)))

Implementing AST in C

Grammar:

$\begin{aligned} E &::= E + T \mid E - T \mid T \\ T &::= (E) \mid \text{id} \mid \text{num} \end{aligned}$

- Define different kinds of AST nodes
 - typedef enum {PLUS, MINUS, ID, NUM} ASTNodeTag;
- Define AST node

```
typedef struct ASTnode {
    AstNodeTag kind;
    union { symbol_table_entry* id_entry;
           int num_value;
           struct ASTnode* opds[2];
           } description;
};
```
- Define AST node construction routines
 - ASTnode* mkleaf_id(symbol_table_entry* e);
 - ASTnode* mkleaf_num(int n);
 - ASTnode* mknode_plus(struct ASTnode* opd1, struct ASTnode* opd2);
 - ASTnode* mknode_minus(struct ASTnode* opd1, struct ASTnode* opd2);

Implementing AST in Java

Grammar: $E ::= E + T \mid E - T \mid T$
 $T ::= (E) \mid id \mid num$

□ Define AST node

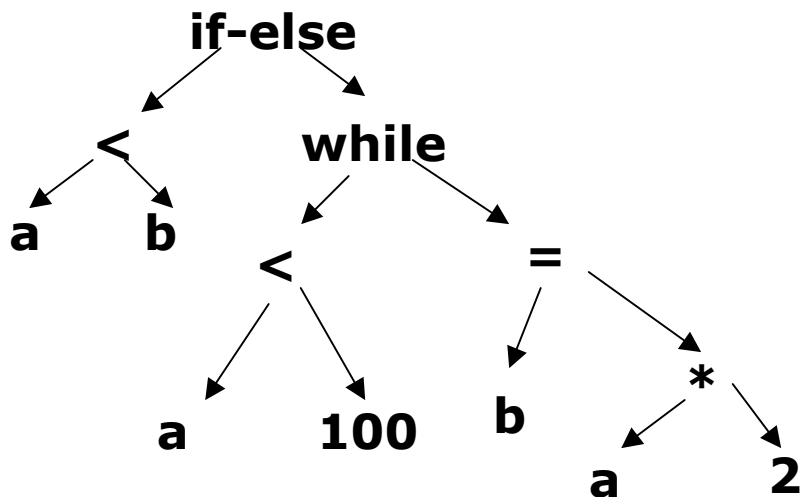
```
abstract class ASTexpression {
    public System.String toString();
}
class ASTidentifier extends ASTexpression
    { private symbol_table_entry id_entry; ... }
class ASTvalue extends ASTexpression
    { private int num_value; ... }
class ASTplus extends ASTexpression
    { private ASTnode opds[2]; ... }
class ASTminus extends ASTexpression
    { private ASTnode opds[2]; ... }
```

More ASTs

Abstract syntax:

```
S ::= if-else E S S | while E S | E | _  
E ::= var | num | true | false | E bop E | uop E  
bop ::= < | <= | > | >= | && | = | + | * | ....  
uop ::= - | * | & | ...
```

Abstract syntax tree



```
class ASTstmt {...}  
class ASTifElse extends ASTstmt {  
    private ASTexpr* cond;  
    private ASTstmt* tbranch;  
    private ASTstmt* fbranch; ...}  
class ASTwhile extends ASTstmt {  
    private ASTexpr* cond;  
    private ASTstmt* body;...}  
class ASTexpr extends ASTstmt {...}  
class ASTvar extends ASTexpr {...}
```

Three address code

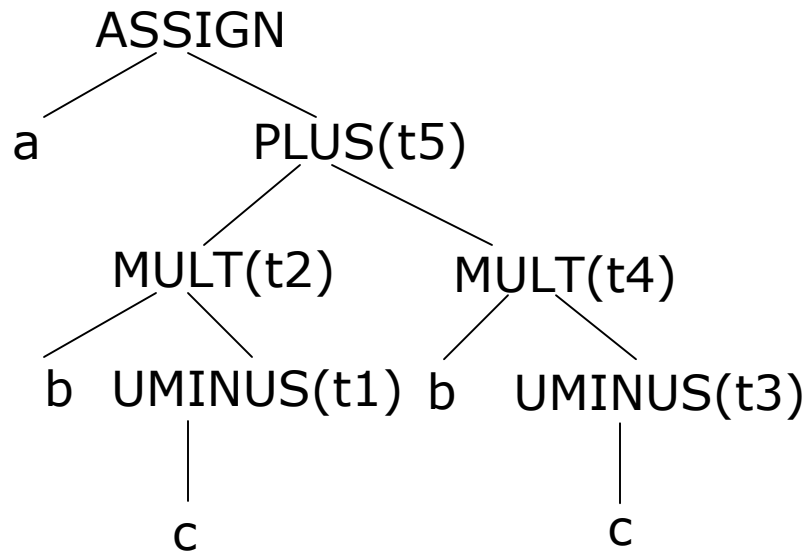
- Low level IL before final code generation
 - Linear representation of AST
 - Every instruction manipulates at most two operands and one result
- Assignment statements
 - $x := y \text{ op } z$, where op is a binary operation
 - $x := \text{op } y$, where op is a unary operation
 - Copy statement: $x := y$
 - Indexed assignments: $x := y[i]$ and $x[i] := y$
 - Pointer assignments: $x := \&y$ and $x := *y$
- Control flow statements
 - Unconditional jump: goto L
 - Conditional jump: if x relop y goto L ; if x goto L; if False x goto L
 - Procedure calls: call procedure p with n parameters

```
param x1
param x2
...
param xn
call p, n
```

Example: translating expressions

Input: $a := b * -c + b * -c$

Abstract syntax tree:



Three-address code:

```
t1 := -c
t2 := b * t1
t3 := -c
t4 := b * t3
t5 := t2 + t4
a := t5
```

Storing three-address code

- Store all instructions in a quadruple table
 - Every instruction has four fields: op, arg1, arg2, result
 - The label of instructions → index of instruction in table

Three-address code

```
t1 := - c
t2 := b * t1
t3 := -c
t4 := b * t3
t5 := t2 + t4
a := t5
```

Quadruple entries

	op	arg1	arg2	result
(0)	Uminus	c		t1
(1)	Mult	b	t1	t2
(2)	Uminus	c		t3
(3)	Mult	b	t3	t4
(4)	Plus	t2	t4	t5
(5)	Assign	t5		a

Translating assignment statement


- For every non-terminal expression E
 - E.place: temporary variable used to store result
- Synthesized attributes
 - Bottom up traversal ensures E.place assigned before used
 - Can reuse temporary variables to reduce size of symbol table


Code concatenation


```
S ::= id '=' E {gen(ASSIGN, E.place, 0, lookup_place(id));}
E ::= E1 '+' E2
    {E.place=new_tmp(); gen(ADD, E1.place, E2.place, E.place);}
E ::= E1 '*' E2
    {E.place=new_tmp(); gen(MULT, E1.place, E2.place, E.place);}
E ::= '-' E1
    {E.place = new_tmp(); gen(UMINUS, E1.place, 0, E.place); }
E ::= (E1) { E.place = E1.place; }
E ::= id { E.place = lookup_place(id); }
```

Control-flow translation of boolean expressions

- Two translation options
 - Same as translating regular expressions
 - Translate into control-flow branches
- For every boolean expression E
 - E.true: the label to goto if E is true
 - E.false: the label to goto if E is false

E: $a < b$  if $a < b$ goto E.true
goto E.false

E: $a < b$ and $c < d$  if $a < b$ goto L1
goto E.false
L1: if $c < d$ goto E.true
Goto E.false

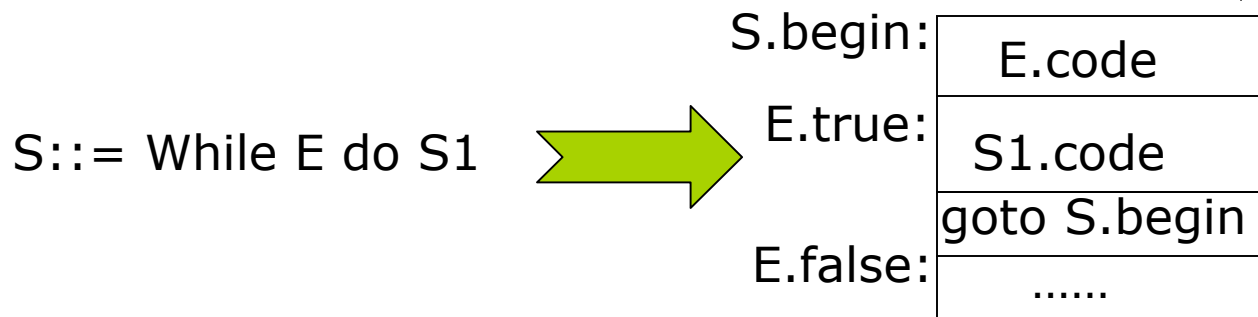
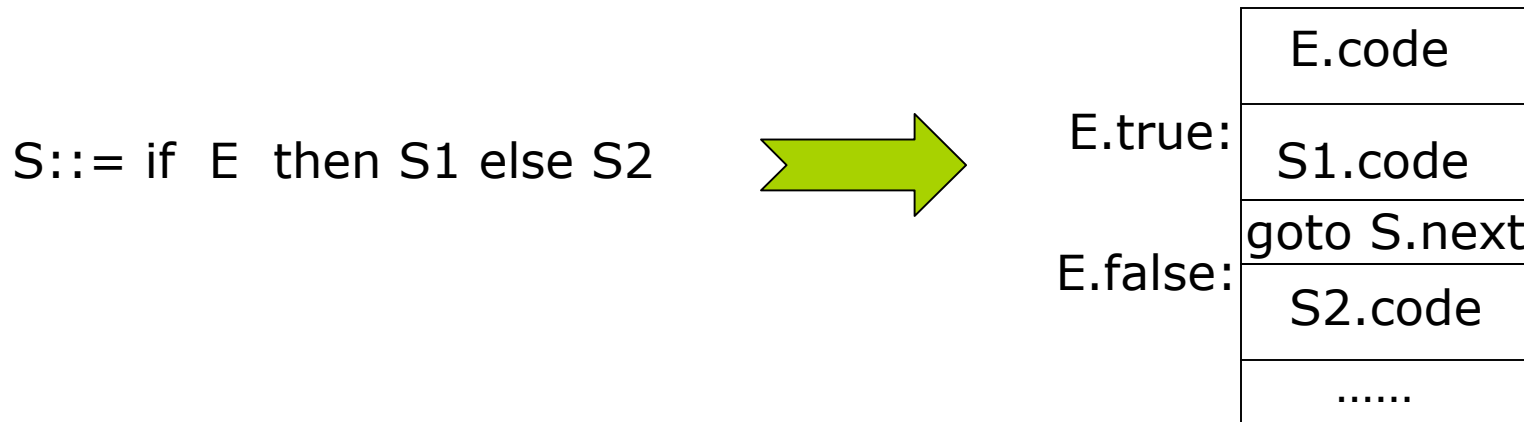
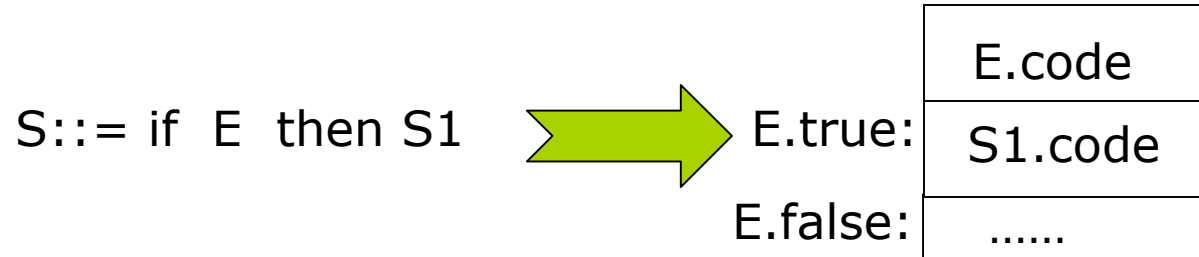
E: $a < b$ or $c < d$  if $a < b$ goto E.true
goto L1
L1: if $c < d$ goto E.true
goto E.false

Translation schemes for boolean expressions

- For every boolean expression E
 - E.true: the label to goto if E is true
 - E.false: the label to goto if E is false

```
E ::= {E1.true=E.true; E1.false=new_label(); } E1 or
      {E2.true=E.true; E2.false=E.false; gen_label(E1.false) } E2
E ::= {E1.true=new_label(); E1.false=E.false; } E1 and
      {E2.true=E.true; E2.false=E.false; gen_label(E1.true) } E2
E ::= {E1.true=E.false; E1.false=E.true;} not E1
E ::= '(' {E1.true=E.true; E1.false=E.false; } E1 ')'
E ::= id1 relop id2
      { gen(IF,id1.place,id2.place,E.true); gen(GOTO,0,0,E.false);}
E ::= true { gen(GOTO,0,0,E.true); }
E ::= false { gen(GOTO,0,0,E.false); }
```

Translating control-flow statements



Translating control-flow statements

- For every statement S
 - S.begin: the label of S; S.next: the label of statement following S
- For every boolean expression E
 - E.true: the goto label if E is true; E.false: the goto label if E is false

```
S ::= IF {E.true=new_label(); E.false=S.next; } E THEN
      {S1.next=S.next; gen_label(E.true); } S1
S ::= IF { E.true=new_label(); E.false=new_label(); } E THEN
      { S1.next=S.next; gen_label(E.true)} S1 ELSE
      {S2.next=S.next; gen(GOTO,0,0,S.next); gen_label(E.false) } S2
S ::= WHILE {S.begin=new_label(); E.true=new_label(); E.false=S.next;
            gen_label(S.begin) } E
      DO {S1.next=S.begin; gen_label(E.true)} S1
      { gen(GOTO,0,0,S.begin); }
S ::= {S1.next=new_label(); } S1
      {S2.next=S.next; gen_label(S1.next) } S2
```

Translating control-flow statements

- Make two passes of the AST
 - First pass
 - Generate three-address code with symbolic labels
 - `new_label()`: create a new symbolic label (placeholder)
 - Determine place of every label
 - `gen_label(symLabel)`: set place of `symLabel`
 - Second pass
 - Replace every symbolic label (placeholder) with the corresponding address in quadruple table