

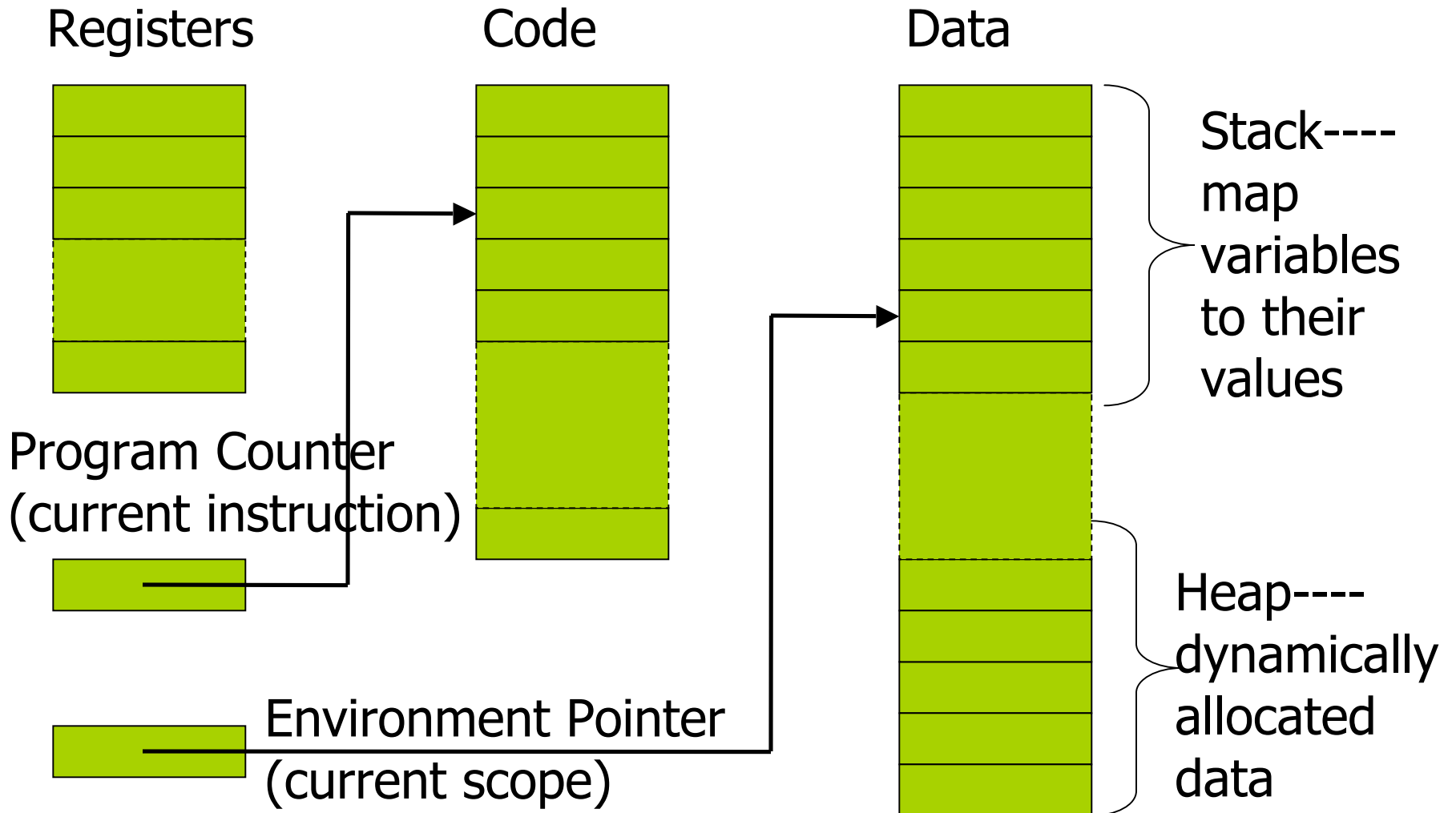
Scope, Functions, and Storage Management



Implementing Functions and Blocks

Simplified Machine Model

(Compare To List Abstract Machine)



Data Storage Management

- Runtime stack: mapping variables to their values
 - When introducing new variables: push new stores to stack
 - When variables are out of scope: pop outdated storages
- Environment pointer: current stack position
 - Used to keep track of storages of all active variables
- Heap: dynamically allocated data of varying lifetime
 - Variables that last throughout the program
 - Data pointed to by variables on the runtime stack
 - Target of garbage collection
- The code space: the whole program to evaluate
- Program counter: current/next instruction to evaluate
 - keep track of instructions being evaluated
- Registers: temporary storages for variables

Blocks in C/C++

```
outer block {  
    {  
        int x = 2;  
        {  
            int y = 3;  
            x = y+2;  
        }  
    }  
}
```

inner block

- Blocks: regions of code that introduces new variables
 - Enter block: allocate space for variables
 - Exits block: some or all space may be deallocated
- Blocks are nested but not partially overlapped
 - Jumping out of a block
 - Make sure variables are freed before exiting
 - What about jumping into the middle of a block?
 - Variables in the block have not yet been allocated

Blocks in Functional languages

- ML:

```
let fun g(y) = y + 3
in
  let
    fun h(z) = g(g(z))
  in h(3)
  end
end;
```

- Lisp:

```
( (lambda (g)
  ((lambda (h) (h 3)) (lambda (z) (g (g z))))
  (lambda (y) (+ y 3)))
```

Summary of Blocks

- Blocks in common languages
 - C { ... }
 - Algol begin ... end
 - ML let ... in ... end
- Two forms of blocks
 - In-line blocks
 - Blocks associated with functions or procedures
- Topic: block-based memory management

Managing Data Storage In a Block

- Local variables
 - Declared inside the current block
 - Enter block: allocate space
 - Exit block: de-allocate space
- Global variables
 - Declared in a previously entered block
 - Already allocated before entering current Block
 - Remain allocated after exiting current block
- Function parameters
 - Input parameters
 - Allocated and initialized before entering function body
 - De-allocated after exiting function body
 - Return values
 - Address remembered before entering function body
 - Value set after exiting function body
- Scoping rules: where to find memory allocated for variables?
 - Need to find the block that introduced the variable

Parameter passing

- Each function have a number of formal parameters
 - At invocation, they are matched against actual parameters
- Pass-by name
 - Rename each occurrence of formal parameter with its actual parameter
 - delay of evaluation
 - Used in Lambda calculus and side-effect free languages
- Pass-by-value
 - Replace formal parameter with value of its actual parameter
 - Callee cannot change values of actual parameters
- Pass-by-reference
 - Replace formal parameter with address of its actual parameter
 - Callee can change values of actual parameters
 - Different formal parameters may have the same location

Example: What is the final result?

pseudo-code

```
int f (int x)
{
  x := x+1; return x;
};
main() {
  int y = 0;
  print f(y)+y;
}
```

pass-by-ref



pass-by-value



Standard ML

```
fun f (x : int ref) =
  ( x := !x+1; !x );
val y = ref 0 : int ref;
f(y) + !y;
```

```
fun f (z : int) =
  let val x = ref z in
    x := !x+1; !x
  end;
val y = ref 0 : int ref;
f(!y) + !y;
```

Scoping rules

Finding non-local (global) variables

- Global and local variables

outer block	x	0
h(3)	z	3
	x	1
g(12)	z	3

Which x?

```
{ int x=0;
  fun g(z) = x+z;
  fun h(z) = let x = 1 in
              g(z) end;
  h(3)
};
```

- Static scope

- Find global declarations in the closest enclosing blocks in program text

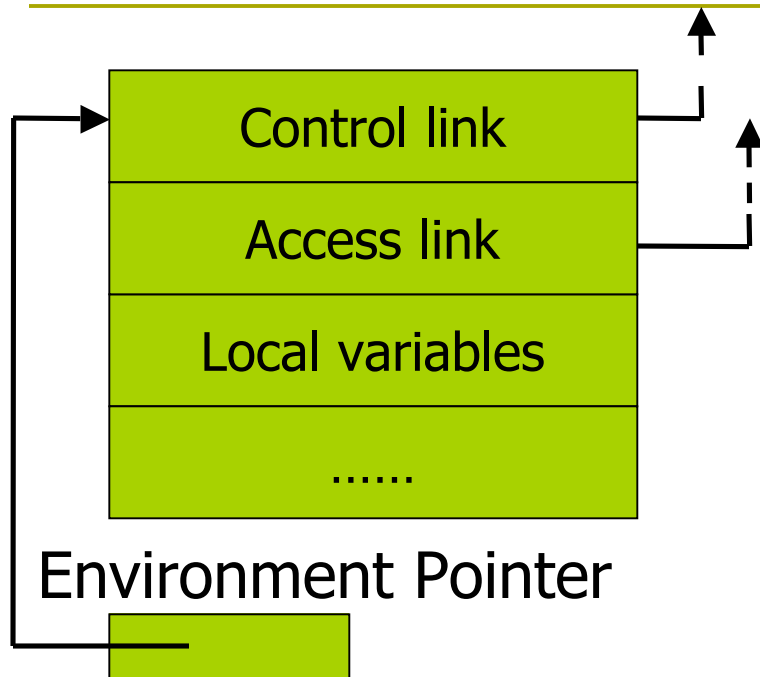
- Dynamic scope

- Find global variables in the most recent activation record

Managing Blocks

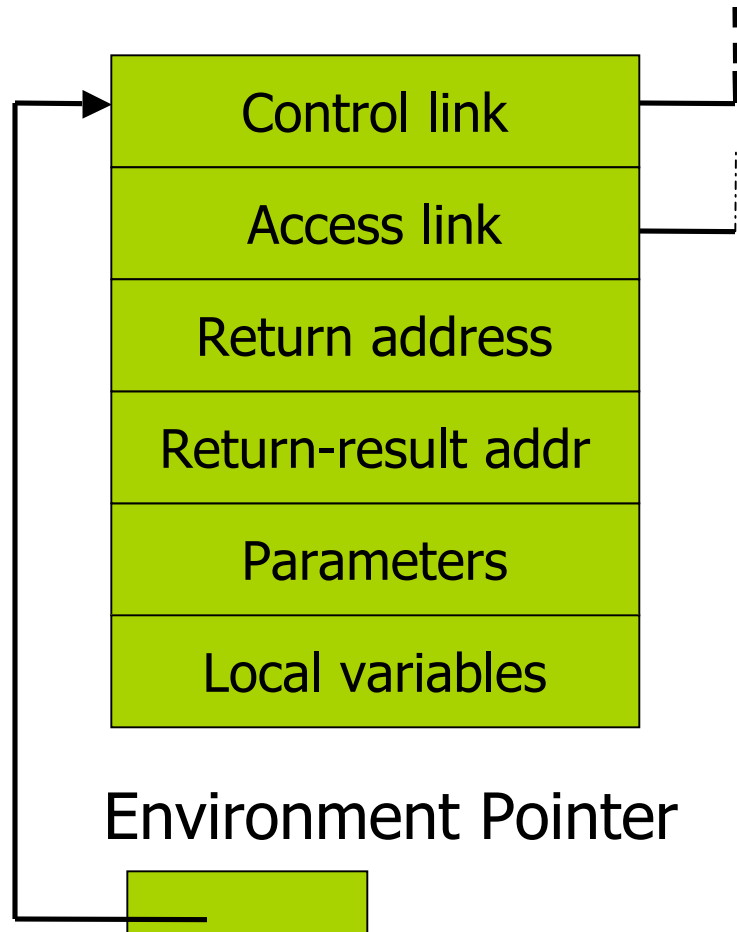
- Activation record: memory storage for each block
 - Contains values for local variables in the block
- Managing Activation Records
 - Allocated on a runtime stack: First-In-Last-Out
 - Before evaluating each block, push its activation record onto runtime stack; after exit the block, pop its activation record off stack
 - Compilers generate instructions for pushing & popping of activation records (pre-compute their sizes)
- Finding locations of local variables
 - Compiler calculate the offset of each variable
 - Dynamically find activation record of introducing block
 - Location = activation record pointer + offset

Activation Record For Inline Blocks



- Control link
 - Point to activation record of previous (calling) block
 - Depend on runtime behavior
 - Support push/pop of ARs
- Access link
 - Point to activation record of immediate enclosing block
 - Depend on static form of program
- Push record on stack
 - Set new control link to env ptr
 - Set env ptr to new record
- Pop record off stack
 - Follow current control link to reset environment pointer

Activation Records For Functions



□ Return address

- Where to continue execution after return
- Pointer to the next instruction following the function call

□ Return-result address

- Where to put return result
- Pointer to caller's activation record

□ Parameters

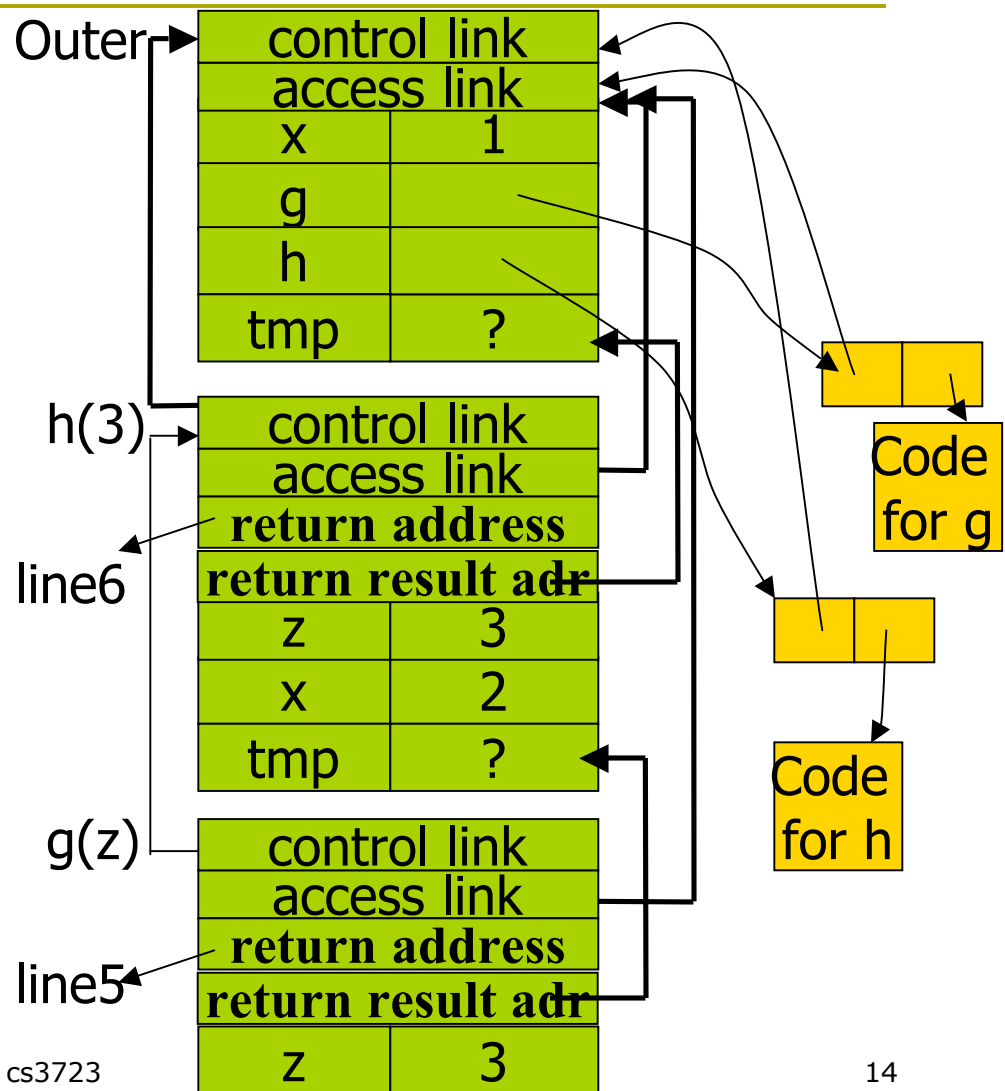
- Values for formal parameters
- Initialized with the actual parameters

Function Abstraction As Values

```

1  let val x=1;
2    fun g(z) = x+z;
3  ← fun h(z) =
4      let x = 2 in
5      g(z) end
6  ← in h(3)
7  end;
    
```

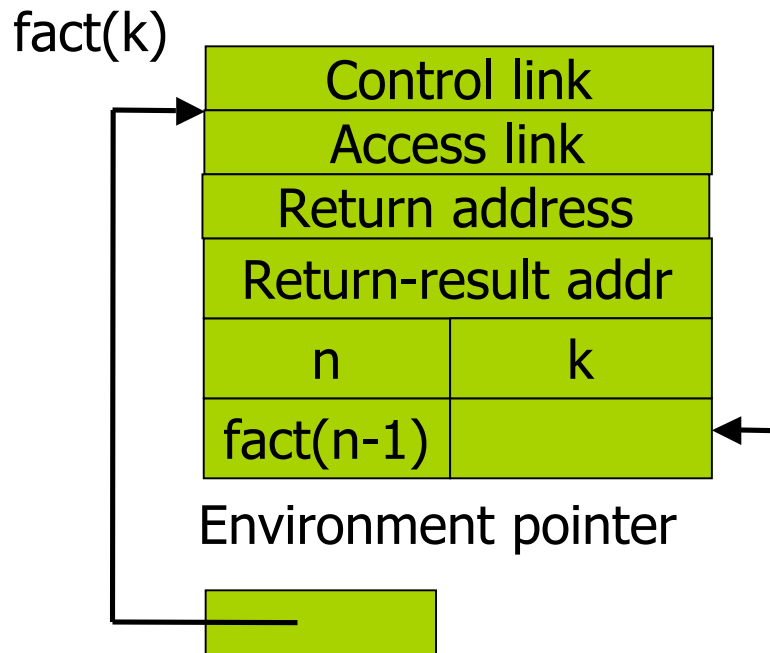
- What are values for g,h?
- How to determine their access links?
 - Inlined blocks
Access link = control link
 - Function blocks
Enclosing block of the function definition



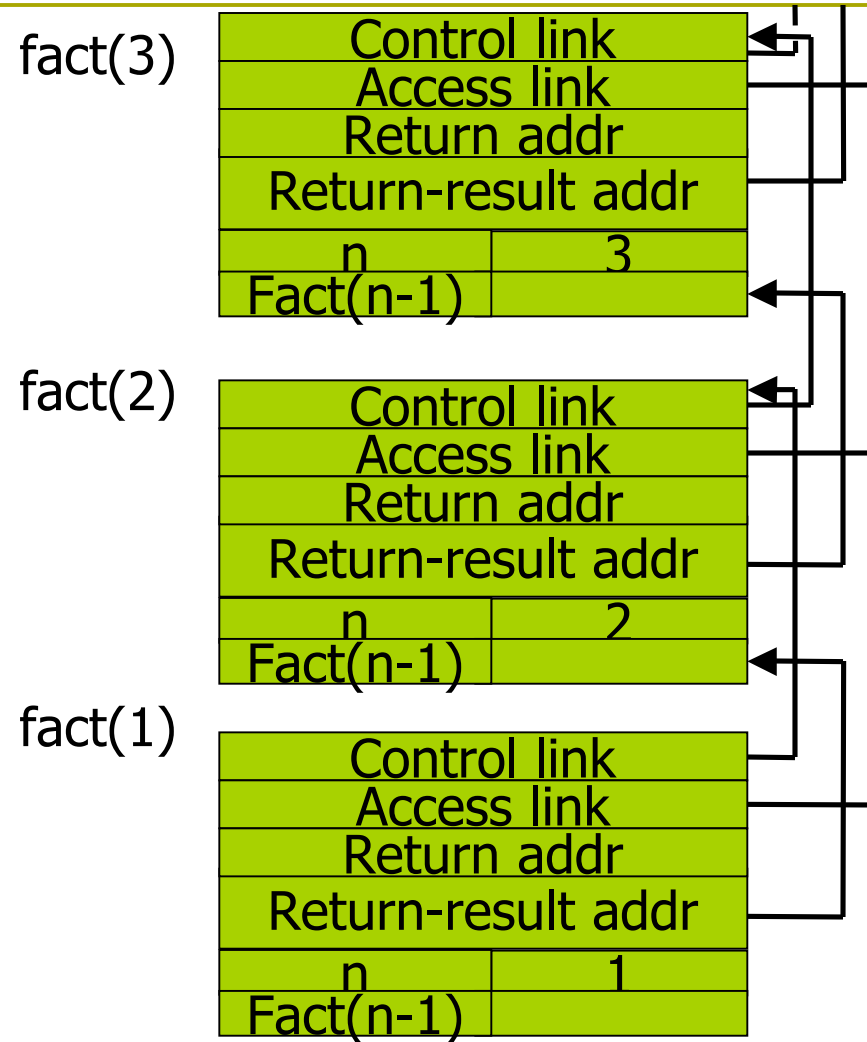
Closures

- A function value is a closure: (env, code)
 - code: a pointer to the function body
 - env: activation record of the enclosing block
- Use closure to maintain a pointer to the static environment of a function body
 - When called, set access link from closure
- When a function is called,
 - Retrieve the closure of the function
 - Push a new activation record onto runtime stack
 - Set return address, return value addr, parameters and local variables
 - Set access link to equal to the env pointer in closure
 - Start the next instruction from code pointer in closure

Example: Function Calls



fact(n) = if $n \leq 1$ then 1
 else $n * \text{fact}(n-1)$



Return Function as Result

- Language feature: functions that return new functions
 - E.g. **fun compose(f,g) = (fn x => g(f x));**
 - Each function value is a **closure = (env, code)**, where code may contain references to variables in env
 - Code is not “created” dynamically (static compilation)
- Use a closure to save the runtime environment of function
 - Environment: pointer to enclosing activation records
 - But the enclosing activation record may have been popped off the runtime stack
 - Returning functions as results is not allowed in C
 - Just like returning pointers to local variables
- Need to extend the standard “stack” implementation
 - Put activation records on heap
 - Invoke garbage collector as needed
 - Not as crazy as it sounds

Tail Call And Tail Recursion

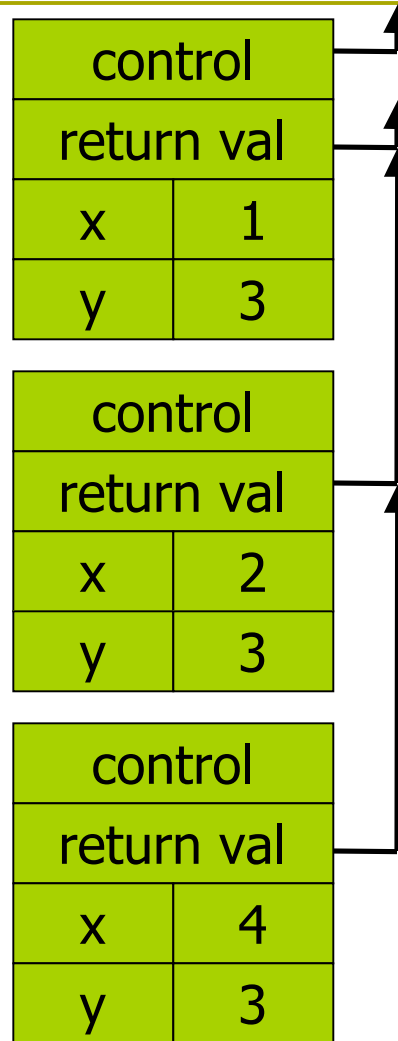
- A function call from g to f is a **tail call**
 - if g returns the result of calling f with no further computation
- Example
 - `fun g(x) = if x>0 then f(x) else f(x)*2`
 - **tail call** (points to `f(x)`)
 - **not a tail call** (points to `f(x)*2`)
- Optimization
 - Can pop activation record on a tail call
 - Especially useful for a **tail recursive call** (f to f)
 - Callee's activation record has exactly same form
 - Callee can reuse activation record of the caller
 - **A sequence of tail recursive calls can be translated into a loop**

Example: what is the result?

f(1,3)

control		↑
return val		↑
x	1	
y	3	

```
fun f(x,y) = if x>y
  then x
  else f(2*x, y);
f(1,3) + 7;
```



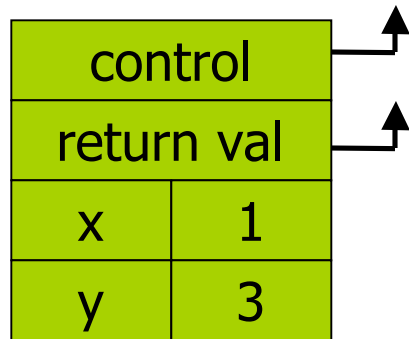
Expressed in loop:

```
fun f(x,y) =
  let val z = ref x in
  while not (!z > y) do
    z := 2 * !z;
  !z
  end;
```

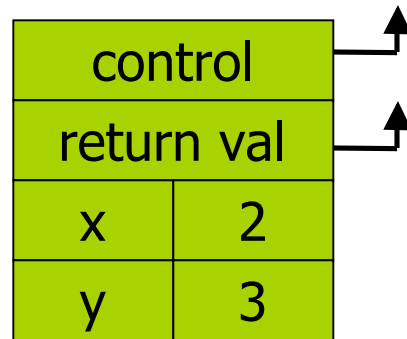
f(1,3) + 7;

Tail recursion elimination

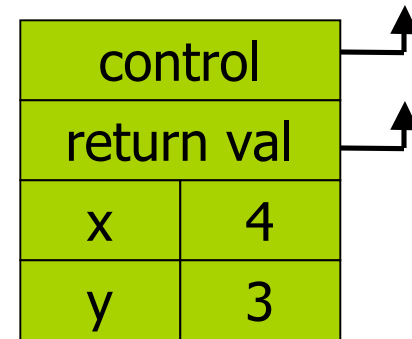
f(1,3)



f(2,3)



f(4,3)



```
fun f(x,y) = if x>y
  then x
  else f(2*x, y);
f(1,3);
```

Optimization: pop followed by push
=> reuse activation record in place

Conclusion: tail recursive function
calls are equivalent to iterative loops

Tail recursion and iteration

□ Tail recursive function

```
fun last(x::nil) = x
  | last( x::y) = last(y);
```

□ Iteration

```
fun last(input) =
  let val y= ref input
  in while not(tl(!y)=nil)
    do
      y := tl(!y)
    end;
  hd(!y)
end
```

□ Step1: what parameters change when making recursive calls?

- create a reference for each changed parameter.
- NOTE: no need to create reference for the return result
 - Tail recursion only returns at the base case

□ Step2: what is the base case of recursion?

- This is the stop condition for the while loop.

□ Step3: what to do before making tail call?

- loop body: prepare for the next tail call

□ Step4: return base case value.

Summary

- Block-structured languages use runtime stack to maintain activation records of blocks
 - Activation records contain parameters, local variables, ...
 - Also pointers to enclosing scope
- Several different parameter passing mechanisms
- Tail calls may be optimized
- Function parameters/results require closures
 - Env pointer of closure used when function is called
 - Runtime stack management may fail if functions are returned as result
 - Closures is *not* needed if functions are not in nested blocks
 - Example: C