

# Intermediate Representation



Abstract syntax tree, control-  
flow graph, three-address code

# Intermediate Code Generation

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- ❑ Intermediate language between source and target
- ❑ Multiple machines can be targeted
  - Attaching a different backend for each machine
  - Intel, AMD, IBM machines can all share the same parser for C/C++
- ❑ Multiple source languages can be supported
  - Attaching a different frontend (parser) for each language
  - Eg. C and C++ can share the same backend
- ❑ Allow independent code optimizations
  - Multiple levels of intermediate representation
    - ❑ Supporting the needs of different analyses and optimizations

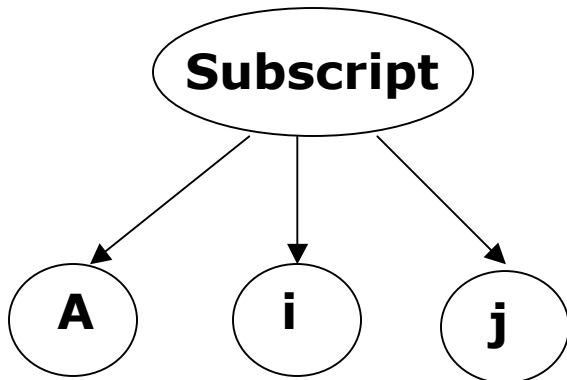
# IR In Compilers

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- Internal representation of input program by compilers
  - Source code of the input program
  - Results of program analysis
    - Control-flow graphs, data-flow graphs, dependence graphs
  - Symbol tables
    - Book-keeping information for translation (eg., types and addresses of variables and subroutines)
- Selecting IR --- depends on the goal of compilation
  - Source-to-source translation: close to source language
    - Parse trees and abstract syntax trees
  - Translating to machine code: close to machine code
    - Linear three-address code
- External format of IR
  - Support independent passes over IR

# Abstraction Level in IR

- Source-level IR
  - High-level constructs are readily available for optimization
    - Array access, loops, classes, methods, functions
- Machine-level IR
  - Expose low-level instructions for optimization
    - Array address calculation, goto branches



Source-level tree

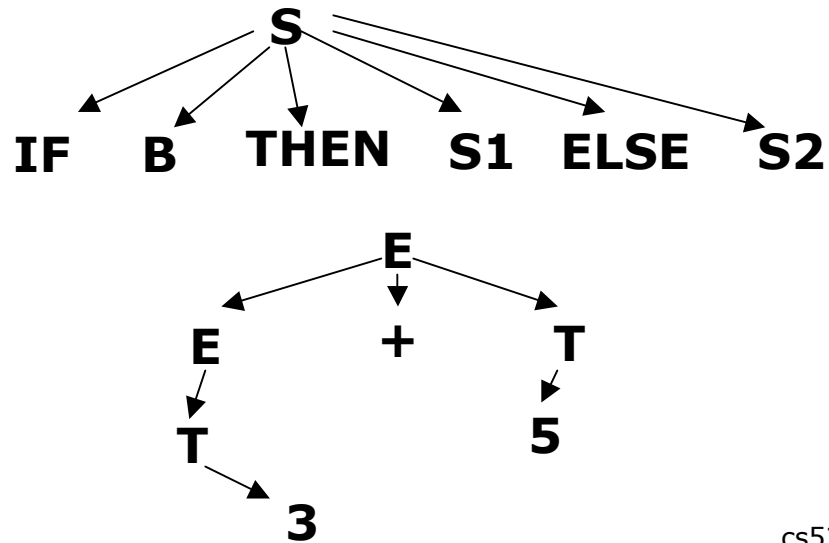
```
loadI 1 => r1
sub rj, r1 => r2
loadI 10 => r3
mult r2, r3 => r4
sub ri, r1 => r5
add r4, r5 => r6
loadI @A => r7
add r7, r6 => r8
load r8 => rAij
```

ILOC code

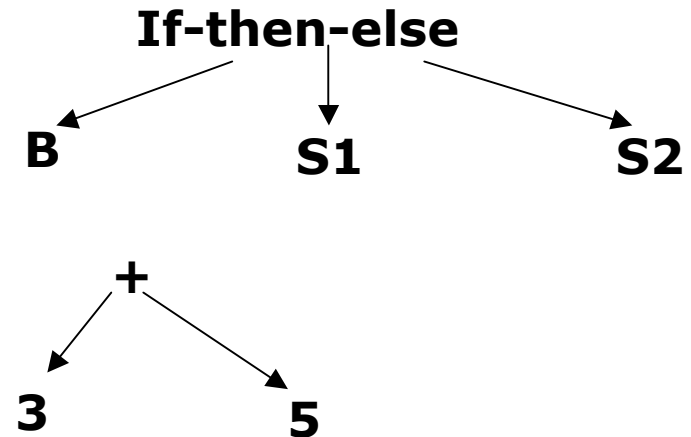
# Parse Tree And AST

- Graphically represent grammatical structure of input program
  - Parse tree: tree representation of syntax derivations
  - AST: condensed form of parse tree
    - Operators and keywords do not appear as leaves
    - Chains of single productions are collapsed

## Parse trees



## Abstract syntax trees



# Implementing AST in C

**Grammar:**

$\begin{aligned} E &::= E + T \mid E - T \mid T \\ T &::= (E) \mid \text{id} \mid \text{num} \end{aligned}$
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- Define different kinds of AST nodes
  - typedef enum {PLUS, MINUS, ID, NUM} ASTNodeTag;
- Define AST node types

```
typedef struct ASTnode {
    AstNodeTag kind;
    union { symbol_table_entry* id_entry;
           int num_value;
           struct ASTnode* opds[2];
           } description;
};
```
- Define AST node construction routines
  - ASTnode\* mkleaf\_id(symbol\_table\_entry\* e);
  - ASTnode\* mkleaf\_num(int n);
  - ASTnode\* mknode\_plus(struct ASTnode\* opd1, struct ASTnode\* opd2);
  - ASTnode\* mknode\_minus(struct ASTnode\* opd1, struct ASTnode\* opd2);

# Implementing AST in Java

**Grammar:**

$\begin{aligned} E &::= E + T \mid E - T \mid T \\ T &::= (E) \mid \text{id} \mid \text{num} \end{aligned}$
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- Define AST node

```
abstract class ASTexpression {
    public System.String toString();
}
class ASTidentifier extends ASTexpression { private symbol_table_entry id_entry; ... }
class ASTvalue extends ASTexpression { private int num_value; ... }
class ASTplus extends ASTexpression { private ASTnode opds[2]; ... }
class ASTminus extends ASTexpression { private ASTnode opds[2]; ... }
```
- Define AST node construction routines
  - ASTexpression mkleaf\_id(symbol\_table\_entry e)  
{ return new ASTidentifier(e); }
  - ASTexpression mkleaf\_num(int n)  
{ return new ASTvalue(n); }
  - ASTexpression mknnode\_plus(ASTnode opd1, struct ASTNode opd2)  
{ return new ASTplus(opd1, opd2); }
  - ASTexpression mknnode\_minus(ASTnode opd1, struct ASTNode opd2)  
{ return new ASTminus(opd1, opd2); }

# Constructing AST

- Use syntax-directed definitions
  - Associate each non-terminal with an AST
    - A pointer to an AST node: E.nptr T.nptr
  - Evaluate synthesized attribute bottom-up
    - From children ASTs, compute AST of the parent

```
E ::= E1 + T    { E.nptr=mknode_plus(E1.nptr,T.nptr); }
E ::= E1 - T    { E.nptr=mknode_minus(E1.nptr,T.nptr); }
E ::= T        { E.nptr=T.nptr; }
T ::= (E)      { T.nptr=E.nptr; }
T ::= id       { T.nptr=mkleaf_id(id.entry); }
T ::= num      { T.nptr=mkleaf_num(num.val); }
```

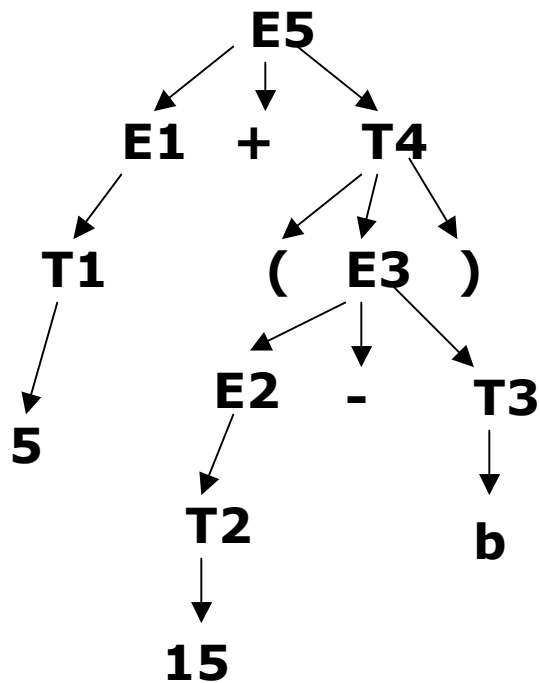
**Exercise: what is the AST for 5 + (15-b)?**  
**What if top-down parsing is used**  
**(need to eliminate left-recursion)?**



# Example: AST for $5+(15-b)$

Bottom-up parsing: evaluate attribute at each reduction

## Parse tree for $5+(15-b)$



1. reduce 5 to T1 using  $T ::= \text{num}$ :  
T1.nptr = leaf(5)
2. reduce T1 to E1 using  $E ::= T$ :  
E1.nptr = T1.nptr = leaf(5)
3. reduce 15 to T2 using  $T ::= \text{num}$ :  
T2.nptr = leaf(15)
4. reduce T2 to E2 using  $E ::= T$ :  
E2.nptr = T2.nptr = leaf(15)
5. reduce b to T3 using  $T ::= \text{num}$ :  
T3.nptr = leaf(b)
6. reduce E2-T3 to E3 using  $E ::= E-T$ :  
E3.nptr = node('-', leaf(15), leaf(b))
7. reduce (E3) to T4 using  $T ::= (E)$ :  
T4.nptr = node('-', leaf(15), leaf(b))
8. reduce E1+T4 to E5 using  $E ::= E+T$ :  
E5.nptr = node('+', leaf(5), node('-', leaf(15), leaf(b)))

# Symbol tables

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- Symbol tables
  - Record information about names defined in programs
    - Types of variables and functions
    - Additional properties (eg., static, global, scope)
  - Contain information about context of program fragment
    - Can use different symbol tables for different purposes
- Naming conflicts
  - The same name may represent different things in different places
    - Use separate symbol tables for names in different scopes
    - Multiple layers of symbol tables for nested scopes
- Implementation of symbol tables
  - Map names to additional information (types, values, etc.)
  - Efficient implementation: using hash tables

# Implementing symbol tables

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- Interface
  - Lookup(name)
    - Returns the record for name if one exists in the table; otherwise, indicates that name is not found
  - Insert(name, record)
    - Stores the information in record in the table for name.
- Symbol tables in nested scopes
  - StartNewScope()
    - Increment the current scope level and creates a new symbol table
  - ExitScope()
    - Changes the current-level symbol table pointer so that it points to the symbol table of surrounding scope
- Use a global symbol table pointer to keep track of the current scope

# Linear IR

- Low level IL before final code generation
  - A linear sequence of low-level instructions
  - Implemented as a collection (table or list) of tuples
- Similar to assembly code for an abstract machine
  - Explicit conditional branches and goto jumps
- Reflect instruction sets of the target machine
  - Stack-machine code and three-address code

## Stack-machine code

```
Push 2
Push y
Multiply
Push x
subtract
```

## two-address code

```
MOV 2 => t1
MOV y => t2
MULT t2 => t1
MOV x => t4
SUB t1 => t4
```

## three-address code

```
t1 := 2
t2 := y
t3 := t1*t2
t4 := x
t5 := t4-t3
```

**Linear IR for  $x - 2 * y$**

# Stack-machine code

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- Also called one-address code
  - Assumes an operand stack
  - Take operands from top of stack; push results onto the stack
  - Need special operations such as
    - Swapping two operands on top of the stack
- Compact in space, simple to generate and execute
  - Most operands do not need names
  - Results are transitory unless explicitly moved to memory
- Used as IR for Smalltalk and Java

**Stack-machine code for  $x - 2 * y$**

<b>Push 2</b>
<b>Push y</b>
<b>Multiply</b>
<b>Push x</b>
<b>subtract</b>

# Three address code

- Each instruction contains at most two operands and one result.
- Typical forms include
  - Arithmetic operations:  $x := y \text{ op } z$  |  $x := \text{op } y$
  - Data movement:  $x := y [z]$  |  $x[z] := y$  |  $x := y$
  - Control flow:  $\text{if } y \text{ op } z \text{ goto } x$  |  $\text{goto } x$
  - Function call:  $\text{param } x$  |  $\text{return } y$  |  $\text{call } \text{foo}$
- Each instruction maps to at most a few machine instructions
- Additional constraints depend on target machine instructions
  - Eg., for  $x := y \text{ op } z$  and  $x := \text{op } y$   
all operands must be in registers → all operands must be temporaries?
- Reasonably compact, while allowing reuse of names and values

**Three-address code for  $x - 2 * y$**

```
t1 := 2  
t2 := y  
t3 := t1*t2  
t4 := x  
t5 := t4-t3
```

# Storing Three-Address Code

- Store all instructions in a quadruple table
  - Every instruction has four fields: op, arg1, arg2, result
  - The label of instructions → index of instruction in table

Three-address code

```
t1 := - c
t2 := b * t1
t3 := -c
t4 := b * t3
t5 := t2 + t4
a := t5
```

Quadruple entries

	op	arg1	arg2	result
(0)	Uminus	c		t1
(1)	Mult	b	t1	t2
(2)	Uminus	c		t3
(3)	Mult	b	t3	t4
(4)	Plus	t2	t4	t5
(5)	Assign	t5		a

**Alternative: store all the instructions in a singly/doubly linked list**  
**What is the tradeoff?**

# Mapping Storages To Variables

- Variables are placeholders for values
  - Every variable must have a location to store its value
    - Register, stack, heap, static storage
  - Values need to be loaded into registers before operation

**x and y are in registers**

**x and y are in memory**

**Three-address code  
for  $x - 2 * y$ :**

```
t1 := 2
t2 := t1*y
t3 := x-t2
```

```
t1 := 2
t2 := y
t3 := t1*t2
t4 := x
t5 := t4-t3
```

**Which variables can be  
kept in registers?  
Which variables must be  
stored in memory?**

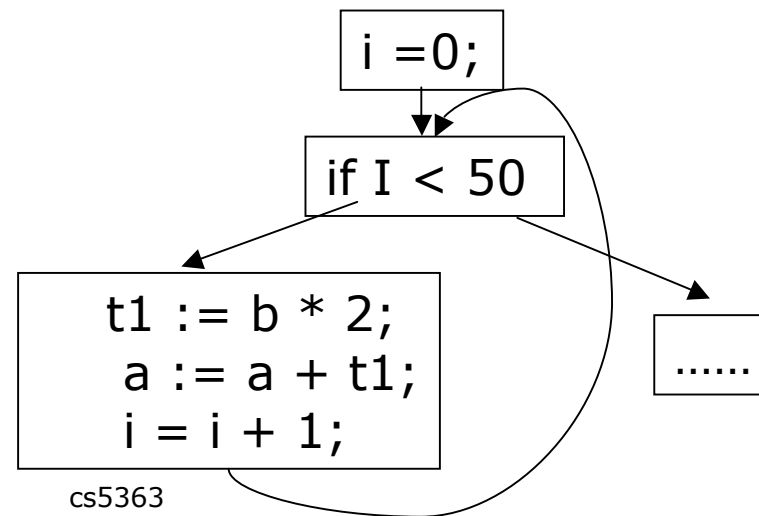
```
void A(int b, int *p)
{
  int a, d;
  a = 3;  d = foo(a);  *p = b+d;
}
```



# Appendix: Control-flow graph

- Graphical representation of runtime control-flow paths
  - Nodes of graph: basic blocks (straight-line computations)
  - Edges of graph: flows of control
- Useful for collecting information about computation
  - Detect loops, remove redundant computations, register allocation, instruction scheduling...
- Alternative CFG: Each node contains a single statement

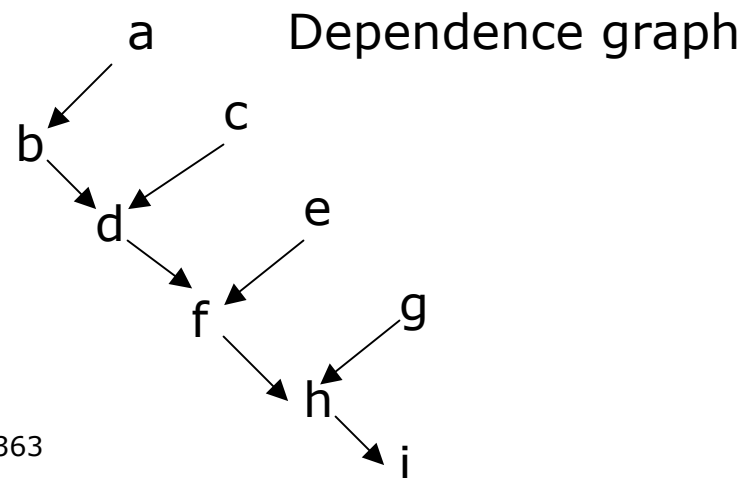
```
.....  
i = 0  
while (i < 50) {  
  t1 = b * 2;  
  a = a + t1;  
  i = i + 1;  
}  
.....
```



# Appendix: Dependence graph

- Graphical representation of reordering constraints between statements
  - Each node  $n$  is a single operation/statement
  - Edge  $(n_1, n_2)$  indicates  $n_2$  uses result of  $n_1$ 
    - The order of evaluating  $n_1, n_2$  cannot be reversed
  - Graph is acyclic within each basic block; is cyclic if loops exist
- Used in reordering transformations
  - Instruction scheduling, loop transformations
- Construction
  - For each pair of statements, evaluate ordering constraint

```
a: r1 := w
b: r1 := r1 + r1
c: r2 := x
d: r1 := r1 * r2
e: r2 := y
f: r1 := r1 * r2
g: r2 := z
h: r1 := r1 * r2
i: return r1
```



# Appendix:

## Static Single-Assignment

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- A variable can hold multiple values throughout its lifetime
  - Mapping multiple values to a name can hide opportunities of optimization
- Static single-assignment form (SSA)
  - Each variable is defined by a single operation in the code
  - Each use of variable refers to a single definition
  - Use  $\emptyset$ -functions to merge definitions from different control-flow paths

```
x := ...
y := ...
while (x < 100)
  x := x + 1
  y := y + x
```

**SSA:**

```
x0 := ...
y0 := ...
if (x0 < 100) goto loop
goto next
loop: x1 :=  $\emptyset(x0,x2)$ 
      y1 :=  $\emptyset(y0,y2)$ 
      x2 := x1 + 1
      y2 := y1 + x2
      if (x2 < 100) goto loop
next: x3 :=  $\emptyset(x0,x2)$ 
      y3 :=  $\emptyset(y0,y2)$ 
```